

P815

12.3

57. a) $q_1 = 5 \quad r = 2$

$$q_n = 5(2)^{n-1}$$

b) $S_4 = q_1 \left(\frac{1-r^4}{1-r} \right) = 5 \left(\frac{1-2^4}{1-2} \right) = 75$

75 skydivers in 4 days

58) a) $q_1 = 32 \left(\frac{1}{2} \right)^{n-1}$

$1 \leq n \leq 6$ are logical values

because $q_6 = 1$

b) $S_6 = q_1 \left(\frac{1-r^6}{1-r} \right)$
 $= 32 \left(\frac{1 - \left(\frac{1}{2} \right)^6}{1 - \frac{1}{2}} \right) = 63$

63 games are played in the tournament

59) After the 1st pass 512 items remain

so $q_1 = 512$ and $r = \frac{1}{2}$

$$q_n = 512 \left(\frac{1}{2} \right)^{n-1}$$

b) $1 = 512 \left(\frac{1}{2} \right)^{n-1} \leftarrow \text{Find } n \text{ when } q_n = 1$

$$\frac{1}{512} = \frac{1}{2}^{n-1}$$

$$\log \left(\frac{1}{512} \right) = (n-1) \log \frac{1}{2}$$

$$\frac{(\log \left(\frac{1}{512} \right))}{(\log \left(\frac{1}{2} \right))} + 1 = n = 10$$

after 10th pass only one term remains

60. $q_1 = 1$ $r = 8$

$$q_n = 1(8)^{n-1}$$

$$q_n = 8^{n-1}$$

$$S_8 = q_1 \left(\frac{1-r^8}{1-r} \right)$$

$$S_8 = 1 \left(\frac{1-8^8}{1-8} \right) = 2,396,745 \text{ squares are removed through stage 8}$$

b) $b_1 = 1 - \frac{1}{9} = \frac{8}{9}$ $r = \frac{8}{9}$

$$b_n = \frac{8}{9} \left(\frac{8}{9} \right)^{n-1}$$

$$b_{12} = \frac{8}{9} \left(\frac{8}{9} \right)^{12-1} \approx 0.2433 \text{ units}^2 \text{ remaining area of the original square after the 12th stage}$$

61. a) For company A

$$q_1 = 20,000, d = 1000$$

$$q_n = q_1 + (n-1)d = 20,000 + (n-1)1000$$

$$q_n = 19,000 + 1000n \quad \text{arithmetic}$$

For company B

$$b_1 = 20,000 \quad r = 1.04$$

$$b_n = q_1 r^{n-1}$$

$$b_n = 20,000(1.04)^{n-1} \quad \text{geometric}$$

c) for company A

$$S_n = n \left(\frac{q_1 + q_n}{2} \right)$$

$$S_{20} = 20 \left(\frac{20,000 + 39,000}{2} \right)$$

$$= 590,000$$

for company B

$$S_n = q_1 \left(\frac{1-r^n}{1-r} \right)$$

$$S_{20} = 20000 \left(\frac{1-1.04^{20}}{1-1.04} \right)$$

$$= 595,561.57$$